Product Heterogeneity and the Distance Puzzle[[1]](#footnote-1)2

Elizaveta Archanskaia[[2]](#footnote-2) and Guillaume Daudin[[3]](#footnote-3)

Abstract

This paper shows that declining exporter-specific product heterogeneity can explain the non-decreasing distance elasticity of trade in 1963-2009. The paper first examines common explanations of the distance puzzle: sample and sectoral composition effects and the rise of FTAs. In the Armington framework, perceived increasing substitutability of exporter-specific product bundles, i.e. the elasticity of trade flows to trade costs, can explain an increase in the distance coefficient. We provide robust empirical evidence that was the case over 1963-2009. Consequently, the well-documented increase in the distance coefficient is compatible with a reduction in the elasticity of trade costs to distance.

*Keywords*: gravity equation, distance puzzle, trade elasticity, trade costs

*JEL codes*: F15, N70

# Introduction

The estimated effect of distance in gravity equations has unambiguously increased over the last 60 years. (Disdier et Head 2008) adopt a meta-analytical approach and find that distance impedes trade by 37% more in the 1990s than it did from 1870 to 1969[[4]](#footnote-4). (Head et Mayer 2013) estimate the distance elasticity of trade in successive cross-sections and find that it has doubled in 1960-2005. This increase in the distance elasticity of trade has been dubbed the “distance puzzle”, as the common opinion is that technological developments in transportation and communication, e.g. the airplane, the container, and the internet, would have led to the “death of distance” by the end of the twentieth century[[5]](#footnote-5).

This paper investigates the empirical relevance of the possibility that within the Armington framework the non-decreasing distance elasticity of trade is due to an increasing sensitivity of consumers to price differences (i.e. a reduction in the perceived heterogeneity of country-specific goods bundles). We make the simple point that the flattening out of the world may go hand in hand with a persistent impeding effect of distance on trade if consumers perceive product bundles shipped out by each country to the world market as increasingly substitutable.

Recent work has sought to rationalize the distance puzzle in three complementary ways: by pointing out a possible misspecification of the econometric model, by refining the specification of the trade cost function, and, more recently, through the lens of network analysis.

The first strand of the literature has investigated the incidence of the estimation method on the magnitude of the distance puzzle. (Santos Silva et Tenreyro 2006) advocate estimating the gravity model in multiplicative form using a specific non-linear estimator, the Poisson Pseudo Maximum Likelihood (PPML). Contrary to the canonical log-linear approach, this estimator provides consistent coefficient estimates and is robust to rounding error and overdispersion which are both likely features of trade data[[6]](#footnote-6). The magnitude of the distance puzzle is reduced when the gravity model is estimated in multiplicative form. Thus, (Bosquet et Boulhol 2009) find that the distance elasticity stays within the .6-.75 range between 1948 and 2006. It is hence more accurate to state the puzzle as a non-decreasing distance elasticity of trade since the 1960s.

The sensitivity of the distance puzzle to the estimation method is likely due to sample composition effects. (Head et Mayer 2013) show that the magnitude of the puzzle in the log-linear specification is reduced in the sample of stable trade partners. Indeed, the growth of trade has been both intensive in the sense that the volume of established trade relations has increased and extensive in the sense that new trade relations have been established (Helpman2008; Baldwin2007). If trade relations have in priority been established between small and distant partners, the reduction in the number of zeros may have gradually reduced the underestimation of the distance coefficient in the loglinear specification[[7]](#footnote-7). This explanation echoes (Felbermayr et Kohler 2006) who pointed out that the log-linear specification was subject to sample selection bias due to the exclusion of zero trade flows. They conjectured that the distance puzzle was an artefact of reduction in this bias through the extensive margin of trade[[8]](#footnote-8).

The second and most prominent strand of the literature singled out the underpinnings of the trade cost function as key to understanding the distance puzzle. The basic point formulated by Buch2004 is that the distance elasticity of trade is invariant to reductions in transportation and communication costs if their distribution over distance remains unchanged Furthermore, while the distance elasticity of transport costs may have decreased (Hummels 2007), other cost components, such as delays, may have become more distance-elastic (Hummels et Schaur 2013). More generally, if freight costs account for an ever smaller fraction of distance-dependent trade costs, the distance elasticity of trade will be determined by other, possibly persistent, cost components[[9]](#footnote-9).

A complementary mechanism is proposed in (Krautheim 2012) in the heterogeneous firms’ framework. He models the informational component of trade costs as a fixed cost which decreases in the number of exporting firms. This refinement of the trade cost function magnifies the distance elasticity of trade because the number of exporters is decreasing in variable trade costs which increase with distance. This magnification mechanism may have been reinforced by the increasing weight of information costs in total fixed costs, explaining increasing elasticities.

An alternative explanation put forward in models with input-output linkages is that the relationship between total trade costs and transport costs may be non-monotonic. An increasing distance elasticity may be an endogenous outcome of transport cost reductions if they engender a reoptimization of the production process which ends up increasing the relative cost of long-distance trade. One possible mechanism is trade cost magnification through multiple border crossings by goods as a consequence of increased production fragmentation (Yi 2010; Daudin, Rifflart, et Schweisguth 2011; Johnson et Noguera 2012). Another mechanism formalized by (Duranton et Storper 2008) works through quality upgrading. Lower transport costs shift trade towards higher-quality inputs which are more distance-sensitive because their customization requires intensive communication, e.g. more back-and-forth travelling, between upstream and downstream firms.

The focus of the literature on the shape of the trade cost function mirrors the expectation that the distance coefficient moves together with the elasticity of trade costs to distance. But (Chaney 2013) provides a theoretical foundation for the gravity equation through the lens of network analysis which demonstrates that the distance coefficient can be invariant to the trade cost function. In this model the rate of distance decay in aggregate trade is linked to the rate of decay in the density of firms which cover that distance with their network of contacts. As the geographic dispersion of the network is increasing in firm size, the shape parameter of the firm size distribution plays a key role in explaining movements in the distance coefficient. Thus, technological advances in transportation increase the geographic dispersion of exports at the level of the firm but have no incidence on the distance elasticity of aggregate trade as long as the stationary firm size distribution verifies Zipf’s law.

The link between the distance coefficient and the parameter which captures the degree of structural heterogeneity in the economy is not specific to (Chaney 2013). Every theoretical foundation of the gravity model delivers a functional relationship of the distance elasticity with the intensity of the incentive to trade, e.g. the degree of structural heterogeneity in some model-specific dimension. The combination of empirical evidence on the changing shape of the trade cost function with evidence on the stability of the distance distribution of trade indicates that structural heterogeneity may have contributed to the evolution of the distance coefficient. However, empirical evidence on the evolution of structural heterogeneity in the economy since the 1960s is notoriously scarce (Head et Mayer 2013).

We pursue the idea that a key parameter for understanding movements in the distance coefficient is the one measuring the degree of structural heterogeneity in the economy. Following (Arkolakis, Costinot, et Rodriguez-Clare 2012), we refer to this parameter as the ‘trade elasticity’. Because of data limitations, we can only estimate the trade elasticity in the Armington framework in which structural heterogeneity captures the degree of product differentiation by place of production (i.e. product heterogeneity). We estimate the distance elasticity of trade and the Armington trade elasticity in each year between 1963 and 2013 and deduce the implied evolution of the elasticity of trade costs to distance[[10]](#footnote-10). Our main result is that the 0.13% increase in the Armington trade elasticity not only rationalizes the non-decreasing distance elasticity of trade but also hints at a reduction in the elasticity of trade costs to distance between 1963 and 2009.

To the best of our knowledge, (Berthelon et Freund 2008) is the only paper that has investigated the impact of changes in perceived product substitutability on the distance coefficient. Using estimates of sectoral Armington elasticities obtained by (Broda et Weinstein 2006), (Berthelon et Freund 2008) find a positive relationship between the variation in sectoral distance coefficients and the variation in Armington elasticities between 1985-1989 and 2001-2005[[11]](#footnote-11). Our approach is different from (Berthelon et Freund 2008) because we focus on the aggregate Armington elasticity and provide direct estimates of this parameter in each year between 1963 and 2013. Our approach is complementary to (Broda et Weinstein 2006) because instead of investigating the degree of differentiation among sectoral varieties we document the increasing similarity of the product mix that countries supply to world markets.

The paper proceeds in three steps. First, we examine the hypothesis that the distance puzzle is a by-product of compositional changes in the set of trading pairs or in the set of traded goods, or in the rise of FTAs. Second, we suggest an *ad hoc* method of measuring structural heterogeneity in the Armington framework. Third, we present the results of this method and conduct a number of robustness checks. We discuss the bias introduced by the presence of zero trade flows. We address endogeneity concerns by instrumenting unit values (our price proxy) with the real exchange rate that is specific to each bilateral relationship. The distance elasticity and the trade elasticity are identified separately in the estimation, while the elasticity of trade costs to distance is deduced from the estimated coefficients. We find robust empirical evidence that this elasticity has increased faster than the distance elasticity of aggregate trade between 1963 and 2013. The evolution of the distance coefficient is thus compatible with a decrease of the elasticity of trade costs to distance.

# The magnitude of the distance puzzle

In this section we evaluate the sensitivity of the distance puzzle in 1963-2009 to composition effects identified as explanatory of movements in the distance coefficient in previous estimations of the loglinearized gravity model. In particular, (Head et Mayer 2013) find that the distance puzzle is reduced in the loglinear specification in the balanced sample between 1960 and 2005 while (Berthelon et Freund 2008)Berthelon2008 find that changes in the sectoral composition of world trade are not explanatory of movements in the distance coefficient in 1985-2005. We find that the distance puzzle is magnified in the sample of stable pairs and robust to fixing the product composition of world trade when the model is estimated in multiplicative form. We also check whether the conduct of trade policy helps rationalize the distance puzzle. If Free Trade Agreements (FTAs) reduce the relative cost of within-FTA trade and FTA formation takes place at short-distance, regional integration would result in an increasing intensity of within-FTA trade, and mechanically induce an increasing distance elasticity of trade costs. This however, is subject to endogeneity concerns.

## The magnitude of the sample composition effect

We use the COMTRADE dataset to make our investigation of the distance puzzle directly comparable to (Head et Mayer 2013) and (Berthelon et Freund 2008). We work with the 4-digit SITC Rev.1 product classification (600-700 goods) because it provides the longest and most comprehensive coverage of disaggregate bilateral trade (1963-2013)[[12]](#footnote-12). Data on bilateral distance, bilateral trade cost controls such as adjacency, common language, colonial linkages, and data on belonging or having once belonged to the same country are taken from the CEPII[[13]](#footnote-13).

We restrict the sample to trade in goods that are attributed to specific 4-digit categories and to pairs for which we have data on bilateral trade cost controls. Appendix **Erreur ! Source du renvoi introuvable.**. lists the resulting set of countries. For each active pair attributed sectoral flows are summed to obtain total bilateral trade. The resulting sample covers between 88% and 99% of reported trade in COMTRADE [[14]](#footnote-14).

Figure 1 summarizes the coverage of the data. The number of active pairs increases more than fourfold in 1962-2013 (in dash, left scale), both because more countries report trade to COMTRADE and because more pairs have non-zero trade flows (Helpman, Melitz, et Rubinstein 2008). Active pairs make up between 45% and 70% of the total number of possible trade relationships, with a clear upward trend (in red, right scale).

Figure 1: Active pairs in COMTRADE (1962-2013)



If we focus on the set of pairs reporting non-zero trade in at least one year of the sample, the share of active pairs increases by 20 percentage points between 1962 and 1990 and by 20 percentage points between 1993 and 2013 (in blue, right scale)[[15]](#footnote-15). By the end of the sample about 2/3 of pairs which trade at least once between 1962 and 2013 are reporting non-zero trade. Hence, sample composition effects are substantial. Nonetheless, the bulk of total trade is attributable to the 1056 pairs that trade both ways in every year. We refer to this set of stable reciprocal pairs as the ‘superbalanced’ sample and use it to investigate the magnitude of the sample composition effect[[16]](#footnote-16).

We follow the canonical (Anderson et van Wincoop 2003) derivation of the gravity model to express aggregate bilateral trade as a function of bilateral trade barriers , multilateral .trade resistance terms in source *i* and destination *j* (resp. ${{\Pi }\_{i}}$ and ), and nominal incomes with $n\in \left\{ i,j,w \right\}$ where *w* is world income[[17]](#footnote-17).

\[{{X}\_{ijt}}\text{ }=\text{ }\left( \frac{{{Y}\_{it}}{{Y}\_{jt}}}{{{Y}\_{w}}t} \right){{\left( \frac{{{\tau }\_{ijt}}}{{{\Pi }\_{it}}{{P}\_{jt}}} \right)}^{{{\epsilon }\_{t}}}}\]

We include the time subscript *t* not only on each variable but also on the elasticity of trade flows to trade costs $\varepsilon $ to underline that this parameter is subject to change. In the Armington framework ${{\varepsilon }\_{t}}=1-{{\sigma }\_{t}}$ where ${{\sigma }\_{t}}$ corresponds to the elasticity of substitution between goods of different national origin. We seek to quantify the evolution of the elasticity of aggregate trade flows to trade costs: ${{\sigma }\_{t}}$ is the key parameter of interest for this paper.

As total bilateral trade costs ${{\tau }\_{ijt}}$ are not directly observed for each pair and year, we model them as a function of observable time-invariant bilateral controls which are distance, adjacency, and common language together with persistent but time-varying controls standard in the gravity literature which are historical and current colonial linkages as well as belonging or having once belonged to the same country. We include an unobserved bilateral trade cost component ${{\nu }\_{ijt}}$ assumed to have mean zero conditional on the observables[[18]](#footnote-18). We denote distance $\eth\_{ij}$, group the other time-invariant observables in the vector *Z* and time-varying observables in the vector $S\_t$ to get the following specification of the trade cost function:

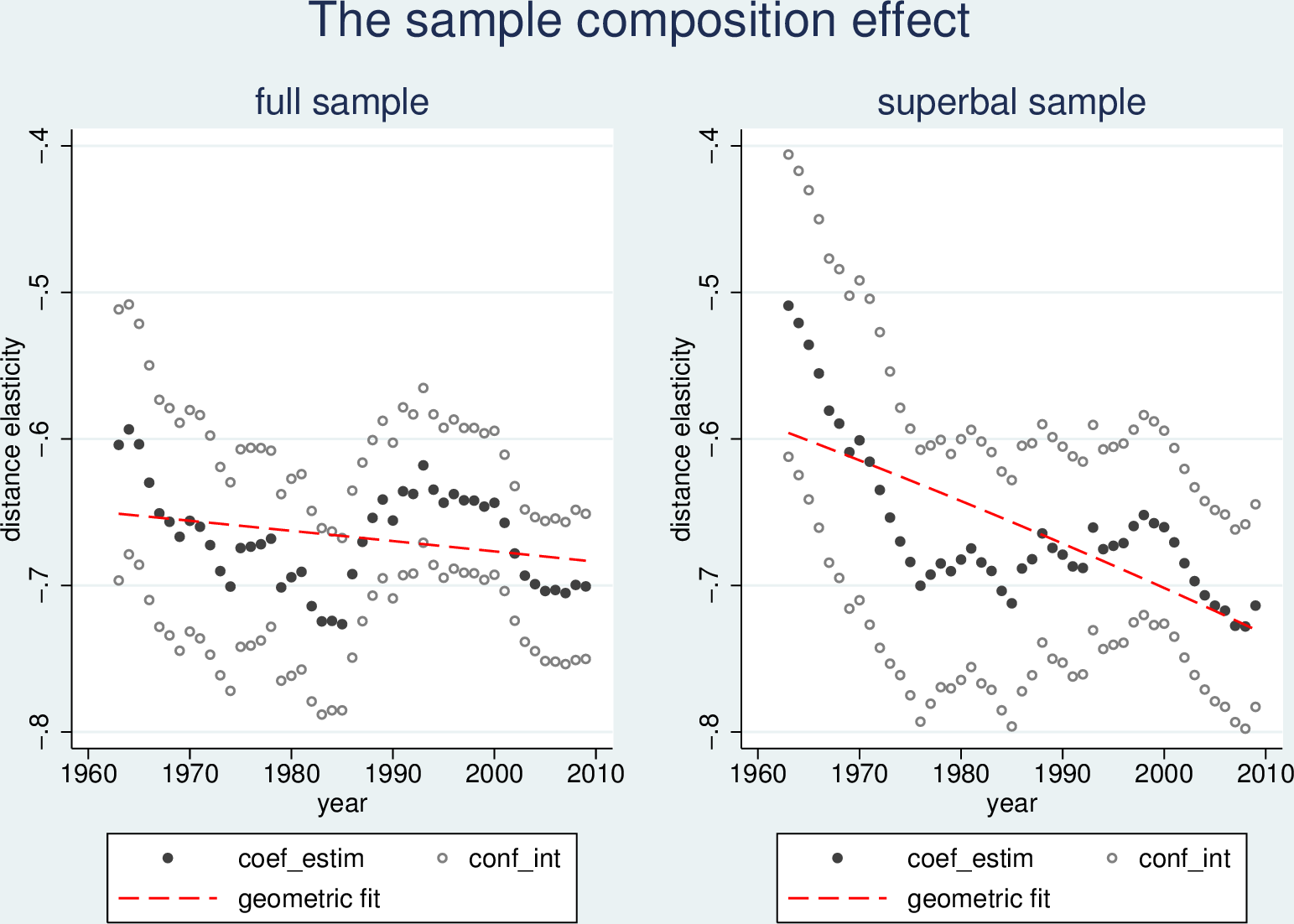
\[{{\tau }\_{ijt}}=\exp \left\{ {{\rho }\_{t}}\ln {{\eth }\_{ij}}+{Z}'{{\zeta }\_{t}}+{{S}\_{t}}^{\prime }{{\varsigma }\_{t}}+{{\nu }\_{ijt}} \right\}\]

Replacing in , substituting source and destination specific variables with country fixed effects (resp. $f\_{it}$ and $f\_{jt}$), defining a constant $\xi\_{t} and specifying a multiplicative error term $\xi }\_{ijt}$ which includes the exponentiated unobserved bilateral trade cost gives the equation to be estimated on aggregate bilateral trade:

\[{{X}\_{ijt}}=\exp \left( {{\xi }\_{t}}-{{\delta }\_{t}}\ln {{\eth }\_{ij}}+{Z}'{{\zeta }\_{t}}+{{S}\_{t}}^{\prime }{{\varsigma }\_{t}}+{{f}\_{it}}+{{f}\_{jt}} \right){{\xi }\_{ijt}}\]

To ensure consistency of the point estimates we do not loglinearize the model although switching to a non-linear estimator may entail a loss of efficiency **(ManningMullahy1999).** We implement equation in the full and superbalanced samples using the PPML estimator (SantosSilvaTenreyro2006). The estimation is conducted in cross section. The parameter of interest is the distance elasticity, $-{{\delta }\_{t}}$, which corresponds to the product of the distance elasticity of trade costs ${{\rho }\_{t}}$ and of the trade elasticity ${{\varepsilon }\_{t}}$[[19]](#footnote-19).

Figure 2 The sample composition effect



Results for both samples are shown in Figure 2 In terms of the point estimates the distance sensitivity of trade has increased by 4.9% in the full sample between 1963-2009 (left pane). This increase is magnified to 22.5% in the superbalanced sample (right pane)[[20]](#footnote-20). There is indeed a distance puzzle, and it is exacerbated in the sample of stable trade relationships[[21]](#footnote-21).

Computing heteroskedasticity-robust standard errors yields the large confidence intervals shown in Figure 2, putting in doubt even the actual existence of the distance puzzle. This is not the case when usual standard errors are used. Considering that the PPML approach already takes into account heterskedasticity, and that we are looking at these point estimates as if they were descriptive statistics on the whole population, we do not believe that invalidates our approach.

## The magnitude of sectoral composition effects

The incidence of sectoral composition effects is assessed in two ways. The first exercise consists in fixing the sectoral composition of world trade. The second exercise consists in fixing the sectoral composition of the bundle supplied by each exporter to the world market.

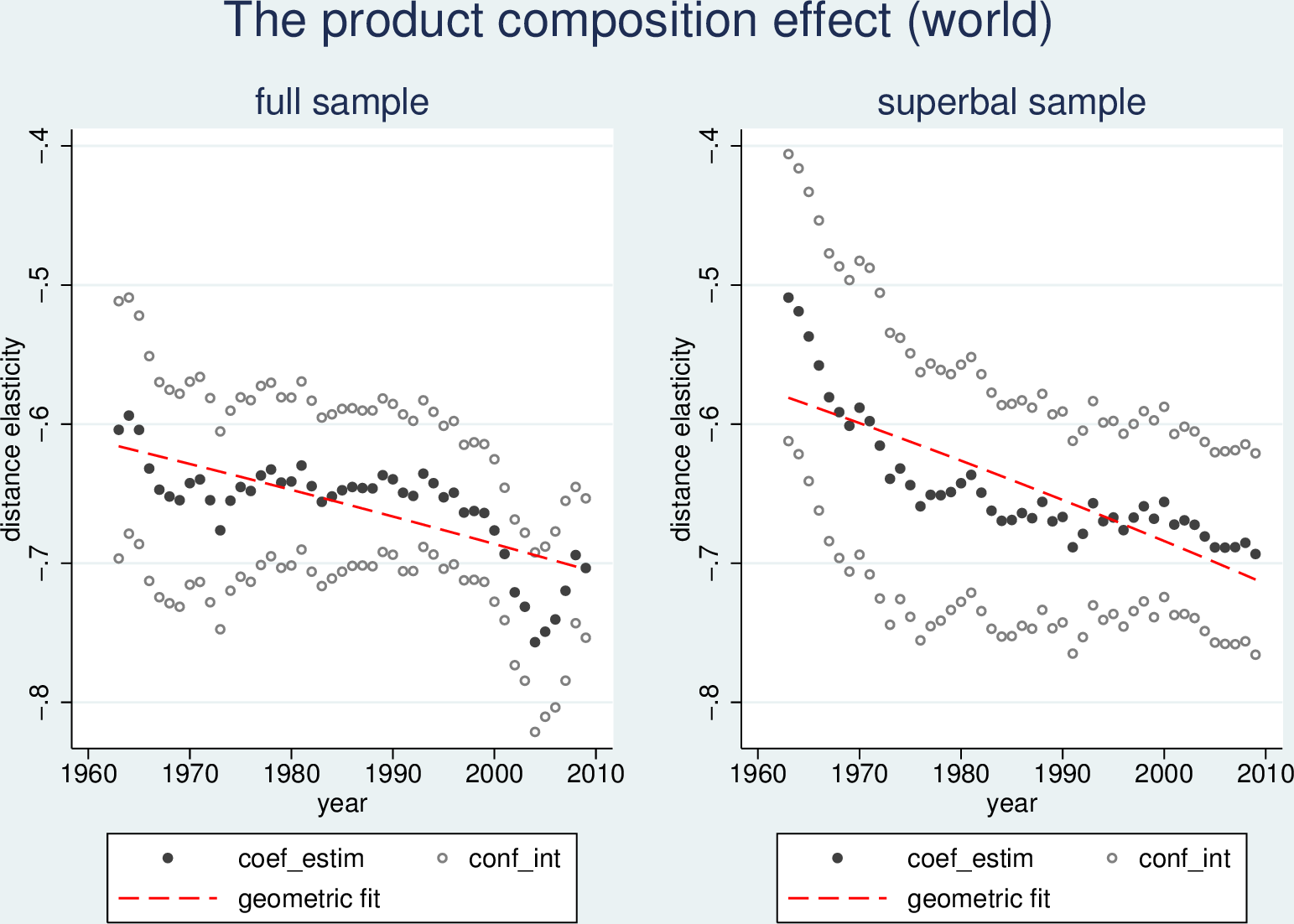
In the first exercise we fix the sectoral composition of total trade to the initial year of the sample. Denoting each 4-digit sector *k* and the annual share of the sector in world trade (*w*,*t*) by $s\_{w,t}^{k}$ , the reweighting procedure fixes the share of each 4-digit sector in world trade to its share in 1963. The reweighted sectoral bilateral flow is:

\[\tilde{X}\_{ijt}^{k}=X\_{ijt}^{k}\*\frac{s\_{w,1963}^{k}}{s\_{w,t}^{k}}\]

The reweighted sectoral flows are summed for each pair, and the gravity equation is estimated in each year for aggregate bilateral trade.

Results are shown in Figure 3. The evolution of the distance coefficient is much linear with time in the full sample (left pane), and this exacerbates the distance puzzle to a 14% increase in ${{\delta }\_{t}}$. The impact of this reweighting procedure is about nil in the sample of stable pairs (right pane) where ${{\delta }\_{t}}$ increases by 22%[[22]](#footnote-22). Indeed, the main incidence of fixing the sectoral composition of world trade is the elimination of short-term fluctuations in the distance coefficient due to fluctuations in the weight of the energy sector. As this sector plays a relatively minor role in trade of stable reciprocal partners, the reweighting procedure has little incidence on the distribution of trade over distance in this sample.

Figure 3: Product composition effect: fixing the world bundle



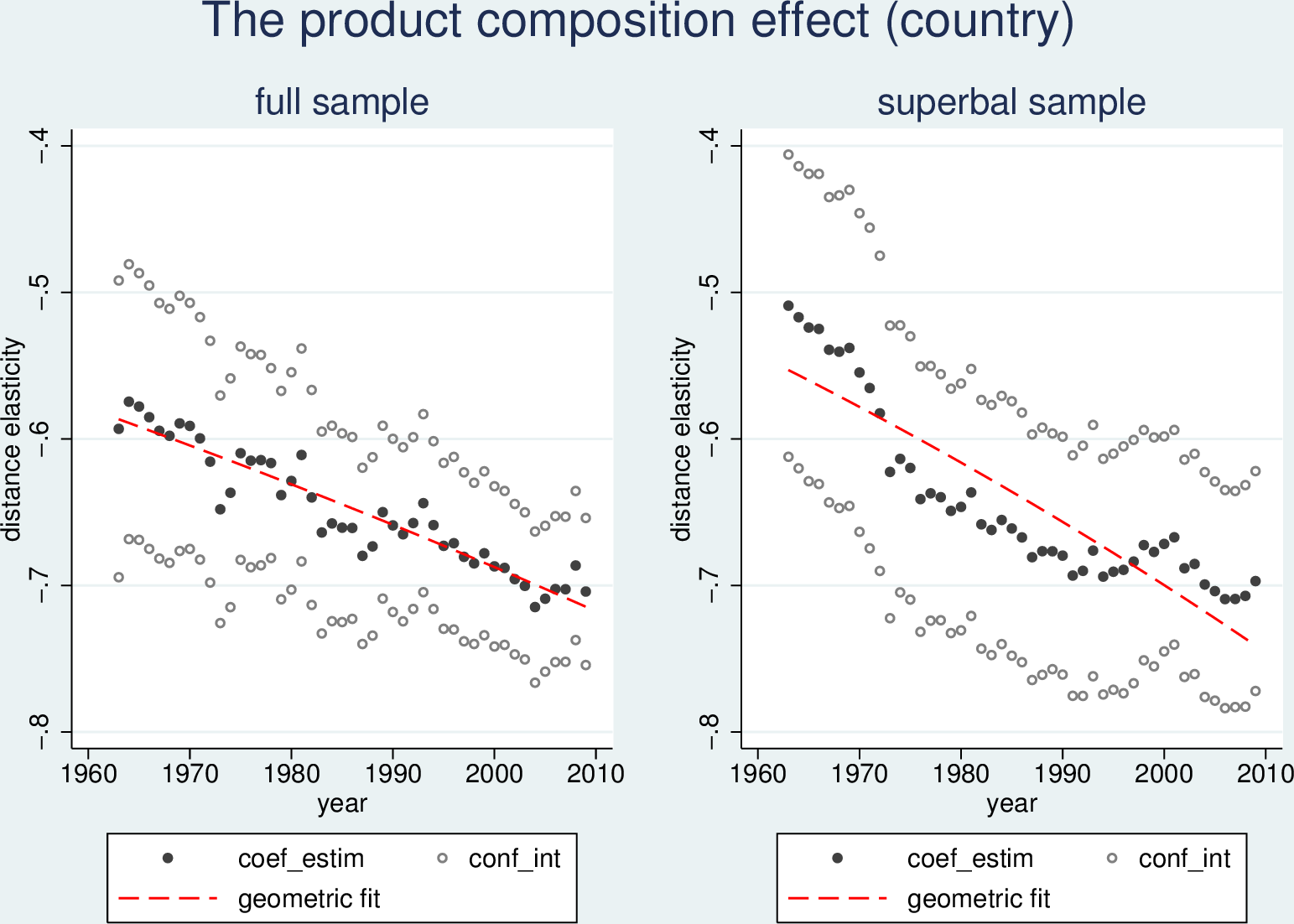
In the second exercise we fix the composition of the bundle supplied by each exporter *i* to the world market. Denoting the annual share of the sector in world imports from *i* by $s\_{i,t}^{k}$, the reweighting fixes the share of each 4-digit sector in world imports from *i* to its share in 1963. The reweighted sectoral bilateral flow is:

\[tilde{X}\_{ijt}^{k}=X\_{ijt}^{k}\*\frac{s\_{i,1963}^{k}}{s\_{i,t}^{k}}\]

The resulting sectoral flows are summed for each pair, and the gravity equation is estimated on total reweighted bilateral trade.

As illustrated in Figure 4, fixing the composition of the country-specific composite good exacerbates the magnitude of the distance puzzle. Furthermore, while the degree of precision in the estimation of the gravity equation is similar to the benchmark specification, 89% of the variation in the distance coefficient is attributable to the time trend in the full sample, against just 8% in the benchmark specification[[23]](#footnote-23). The corresponding annual growth rate is .43% in the full, and .64% in the stable sample. This corresponds to a 22% increase in the distance sensitivity of trade between 1963 and 2009 in the full sample, and to a 34% increase in the stable sample.

Figure 4: Product composition effect: fixing the country bundle



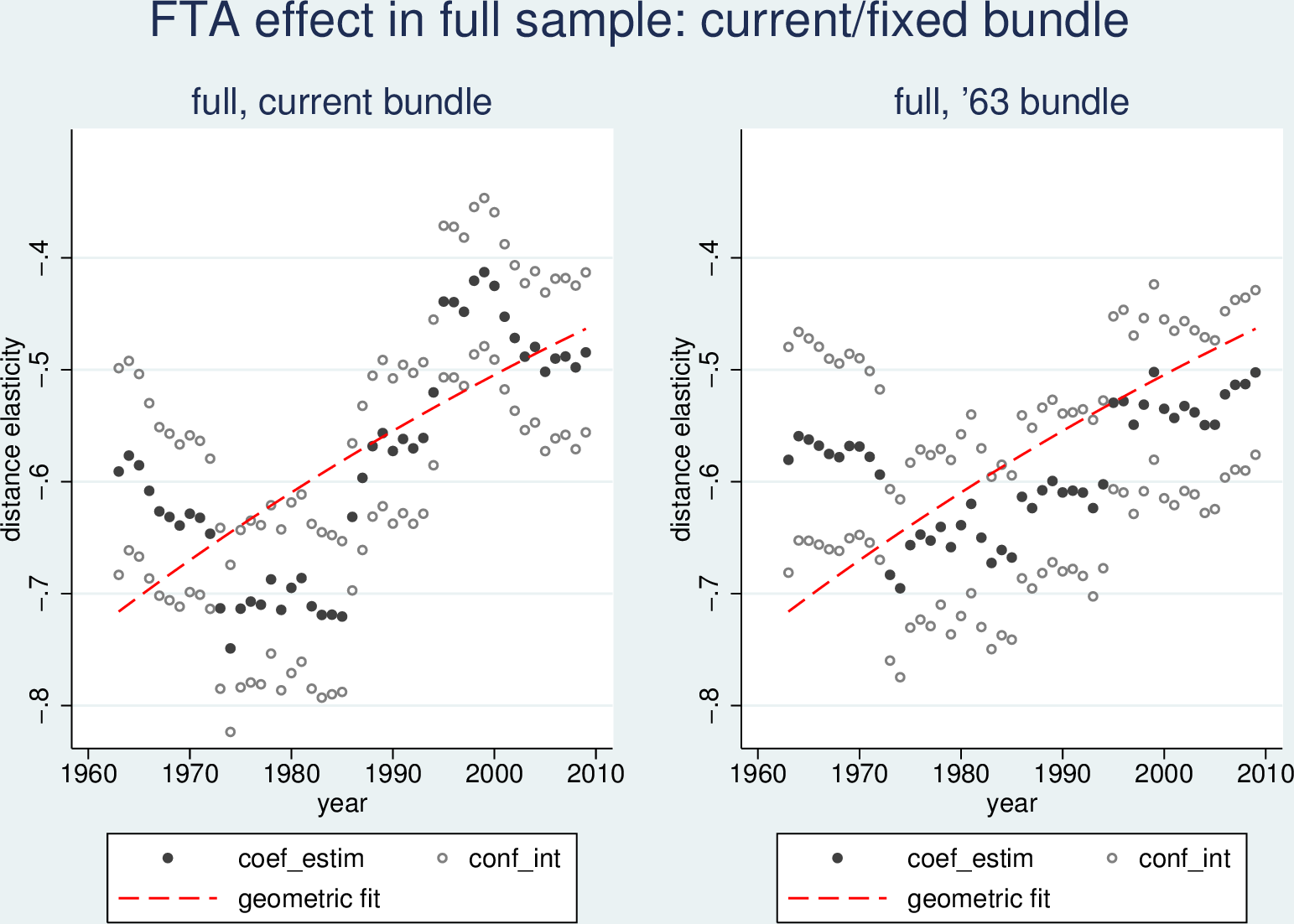
Short-term fluctuations in the distance coefficient are likely to be attributable to product and sample composition effects. But the long-term evolution of the distance elasticity appears linked to structural changes that are reinforced in the set of stable trade relationships.

## The magnitude of the FTA effect

It is possible that policy changes affected the distance distribution of trade costs inducing an increase in the distance elasticity. The distance elasticity of ad valorem tariffs is unlikely to have increased (Berthelon2008). However, institutional and informational trade barriers may have been disproportionately reduced for within-FTA trade and may have resulted in the intensification of short-distance trade if FTAs have predominantly been signed between regional partners.

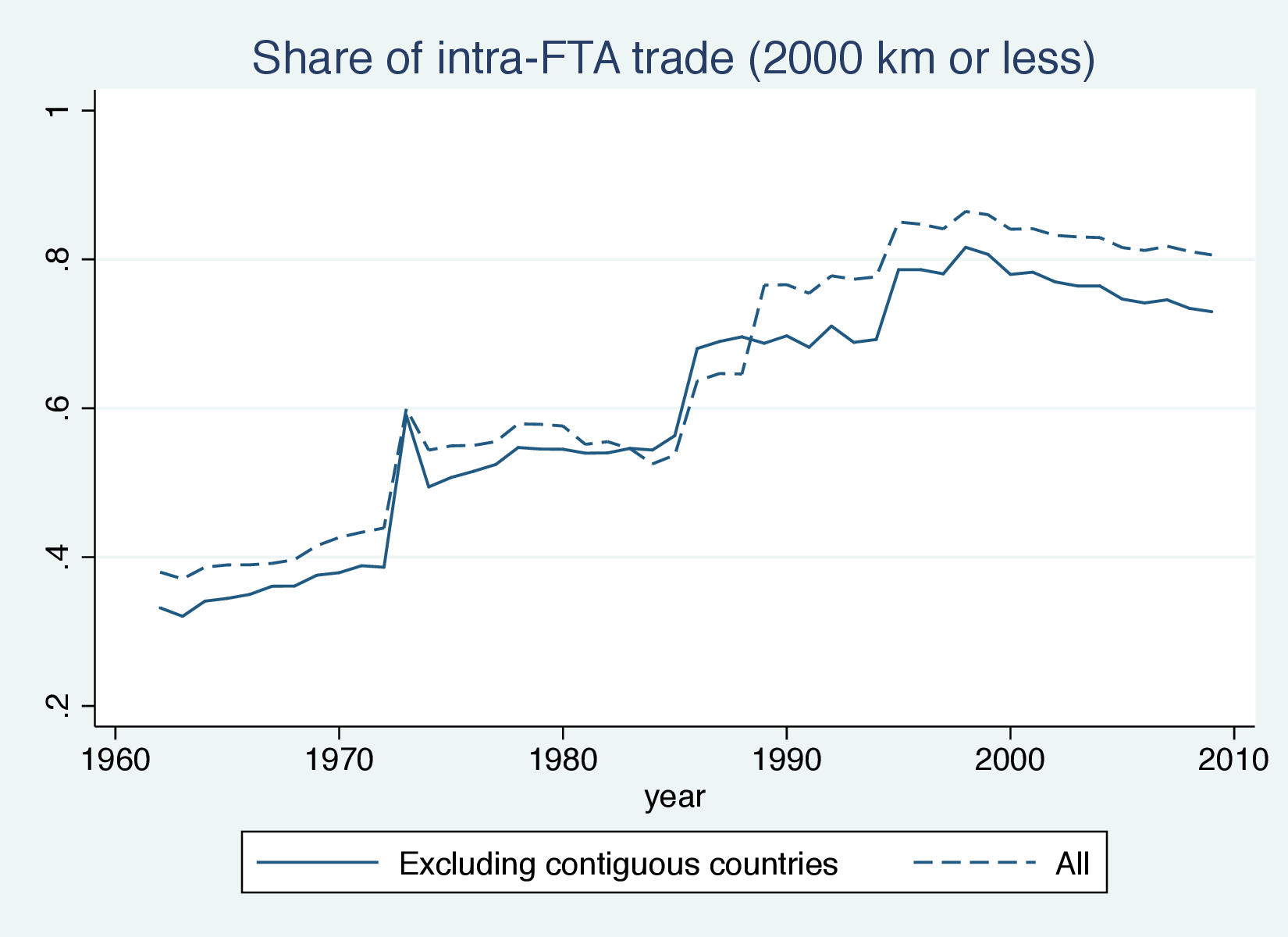
A first pass on the data suggests that is indeed the case. We measure the naively-corrected-for-FTA distance elasticity ${{\delta }\_{naive}}$ by estimating equation in each year while augmenting the vector ${{S}\_{t}}$ with a separate control for each active FTA and an additional control for GATT/WTO membership. This method reverses the direction of change in the distance elasticity (Figure 5). The effect of distance decreases by 1% per year without controlling for sectoral composition effects (left pane), and it decreases by .5% per year when the composition of the country bundle is fixed (right panel)[[24]](#footnote-24).

Figure 5 : Evolution of the distance elasticity with FTA controls



However, this result is not enough to show that the rise of FTA explains the distance puzzle by itself. Figure 6 reports the increase in FTA coverage of trade taking place at less than 2000 km from 40 to 80% in 1963-2009. For the sake of the argument, imagine that FTA have had actually no trade-creating effect and that their coverage has grown to include all nearby-trade in 2009. In that case, an exogenous increase of the distance elasticity manifested by an increase of nearby-trade relative to distant-trade would be completely masked by the introduction of FTA controls.

Figure 6: Share of intra-FTA trade among nearby countries (2000km or less)



One way to explore this objection is to verify the endogeneity of FTA formation. If some, deep, FTA might plausibly have trade-creation effects, others, swallow, FTA might not. (Bosquet et Boulhol 2009) investigates the impact of FTA formation on the distance puzzle while controlling for the endogeneity of country selection into FTAs with the (Baier et Bergstrand 2007) methodology. Constraining the trade creating effect of FTAs to be identical in each year and for all FTAs, (Bosquet et Boulhol 2009) (compare their graph 9 and 11) find that FTAs have had no impact on the evolution of the distance elasticity, even though numerous other papers have found that, when controling for endogeneity, there was a trade-creating effect of FTA ((Baier et Bergstrand 2007), (Egger et al. 2011) (Baier, Bergstrand, et Feng 2014).

## Summing up: the robustness of the distance puzzle

Table 1: Evolution of ${{\delta }\_{t}}$: sample, composition and FTA effects

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
|  | Full sample | | | Stable sample | | |
|  | rate (%) | R-sq | tot.change | rate (%) | R-sq | tot.change |
| Baseline | .10\*\* | .08 | 1.049 | .44\*\*\* | .51 | 1.225 |
| Stable world product bundle | .29\*\*\* | .56 | 1.143 | .44\*\*\* | .67 | 1.224 |
| Stable country product bundle | .43\*\*\* | .89 | 1.218 | .64\*\*\* | .79 | 1.339 |
| FTA | -88\*\*\* | .48 | 0.667 | -1.99\*\*\* | .55 | 0.398 |

Note: Estimated annual growth rates reported in col.2 and col.5 are obtained as a geometric fit on the basis of annual point estimates of the distance coefficient in 1963-2009. Col.3 and col.6 report the share of time variation in the point estimate explained with the annualized growth rate.

Table 1 summarizes our findings. The distance puzzle is exacerbated in the sample of stable pairs and robust to fixing the product composition of world trade. Hence, the non-decreasing distance elasticity is likely to be a structural outcome rather than an artefact of composition effects. FTAs might explain the distance puzzle, but there might also be a simple selection effect, e.g. through the increasing geographic scope of FTAs and their increasing coverage of short-distance trade rather than through the intensification of within-FTA trade. These results motivate our focus on structural heterogeneity as a possible alternative explanation of the non-decreasing distance elasticity.

# Interpreting the distance coefficient

## What does the trade elasticity actually measure?

The distance coefficient is the product of two elasticities: the elasticity of trade costs to distance $\rho $ and the elasticity of trade flows to trade costs $\zeta $. The question addressed in this paper is very simple. Have trade flows become more sensitive to trade costs (increasing $\zeta $), or have trade costs become more sensitive to distance (increasing $\rho $)? In section 3 we estimate the evolution of $\zeta $ to deduce the evolution of $\rho $. The three main microfoundations of the gravity model of trade give structurally different interpretations to $\zeta $ but not to $\rho $. In this section, we provide details on the procedure used in this paper to estimate the evolution of $\zeta $ in the Armington framework.

In (Eaton et Kortum 2002) the heterogeneity dimension captured by the trade elasticity $\zeta $ is intersectoral. Consumers maximize a CES utility function defined at the intersectoral level by shopping around the world for the cheapest supplier of each sectoral good.

In the Melitz-Chaney framework the heterogeneity dimension captured by the trade elasticity $\zeta $ is intrasectoral. Consumers value firm-specific varieties of sectoral goods which they acquire in monopolistic competition markets.

In (Anderson et van Wincoop 2003) there is no heterogeneity in productive efficiency. The production process in each country and sector is constant returns to scale. There is thus perfect competition between domestic producers. The heterogeneity dimension comes from the assumption that consumers perceive products of different national origin as intrinsically imperfect substitutes. Each country is specialized in production of country-specific varieties which on aggregate give a country-specific composite good. The parameter $\zeta $ is the lower tier Armington elasticity of substitution. It measures the degree of substitutability of goods of different national origin.[[25]](#footnote-25)

## What do we know about the evolution of the trade elasticity?

In neither of these models there is a theoretical mechanism to explain a change in the trade elasticity overtime. A shock to consumer preferences or to the shape parameter of the productivity distribution would be required. Nonetheless, the heterogeneity parameter measured on aggregate trade data could have evolved over 1962-2009 without any shock to the underlying heterogeneity, either through changes in the range of traded goods, time-sensitive aggregation issues linked to estimating a single parameter across sectors, or agents’ adaptation to a changing economic environment. However, there is little empirical evidence on the evolution of sector-specific and aggregate trade elasticites in either model.

To the best of our knowledge, there is no direct empirical evidence on the evolution of sectoral or aggregate efficiency dispersion parameters in the heterogenous firms framework. Different theoretically grounded methods have been used to estimate aggregate trade elasticities in the Ricardian framework for a specific year ((Eaton et Kortum 2002; Simonovska et Waugh 2014; Costinot, Donaldson, et Komunjer 2012; Caliendo et Parro 2012), but only (Levchenko et Zhang 2011) study the evolution of intersectoral productivity dispersion. They find evidence of within-country convergence in sectoral knowledge stocks in 1960-2010. As there is less heterogeneity in producer efficiency across the set of goods comparative advantage exerts a weaker force against trade resistance imposed by trade barriers.

Evidence on the evolution of lower-tier Armington elasticities of substitution measured on aggregate data is scarce. For France, (Welsch 2006) provides estimates of aggregate lower-tier Armington elasticities since the 1970s. He finds that among exporters to the French market the elasticity peaked in the 1970s, and progressively decreased in the 1990s. (Broda et Weinstein 2006) provide evidence on the evolution of sectoral Armington lower-tier elasticities between 1972-1988 and 1990-2001 for American imports. They find that they have decreased for all types of goods at all levels of product disaggregation, i.e. at the 10-digit, 5-digit, and 3-digit levels. These results indicate that the parameter estimated on aggregate trade data would also have decreased, deepening the distance puzzle. But to the best of our knowledge, no paper has as yet provided evidence on the evolution of Armington elasticities for aggregate bilateral trade while constraining the parameter to be the same across destination markets.

## A method to measure trade elasticity in the Armington framework

Measuring Armington elasticity is an perennial issue in trade litterature. Feenstra et al. (2014) discusses the difficulties and a state-of-the art method to measure both higher-tier (or "macro") Armington elasticities and lower-tier (or "micro") ones (see also Feenstra (1994), and refinements in Broda and Weinstein (2006) and Imbs and Méjean (2013)). We depart from this litterature and suggest a cruder estimation method for numerous reasons. First, as we want to measure the lower-tier Armington elasticity from 1963 for all the countries involved in world trade, we operate in a data-poor environement. We cannot use dissagregated domestic prices nor production. We believe that the biases entailed by this lack of information do not make the exercice worthless because we are interested in the effect of the evolution of the parameter rather than in its exact value. Second, Feenstra’s method and its developments relies on the assumption the elasticicy parameter remains constant through time, whereas our research question implies that the parameter can vary from year to year. Third, more fundamentally, Feenstra’s elasticity parameter determines short-run, marginal, longitudinal effects whereas we are interested in the elasticity parameter which determines long-run, equilibrium, cross-section outcomes. While we admit that in most tracktable theoretical settings these would be the same. In the absrtact, is not immediate that they should be.

The UN COMTRADE bilateral trade database covers the majority of countries over 1962-2009. It gives information on trade flows and cif unit values at the SITC 4-digit level. This data are sufficient to estimate the trade elasticity in the Armington framework. If we have importer-specific prices in destination markets and importer-specific market share, we should be able to observe some statistical regularities. The basic intuition of the method we use starts from the well-known result that assuming CES utility function in the one-good Armington framework we have:

\[{{X}\_{ij}}={{\left( \frac{{{P}\_{ij}}}{{{P}\_{j}}} \right)}^{-(\sigma -1)}}{{Y}\_{j}}\]

where is the cif value of the exports from i to j, is the cif price of the good shipped from *i* to *j* and is the price index in the destination and total import demand in the destination.[[26]](#footnote-26) The exponent  captures substitutability of country-composite goods across frameworks. It is also the aggregate trade elasticity  in the Armington framework.

Briging this equation to the data is difficult, however, as we do not observe aggregate prices, but unit values at the SITC 4-digit category level. Still, the distance puzzle concerns an elasticity estimated on aggregate trade data. As shown by (Imbs et Méjean 2013) this parameter cannot generally be mimicked by a theoretically grounded weighted average of sector-specific trade elasticities. Hence, we need an estimation procedure that works directly with aggregate data.

Define aggregate imports from source country to destination country as the sum of imports from each sector where a sector corresponds to a SITC 4-digit category: ${{X}\_{ij}}=\sum\limits\_{k}{{{X}\_{k,ij}}}$.[[27]](#footnote-27) Given CES utility at the intersectoral level, sectoral demand in country in sector for imported goods is given by:



\[\begin{array}{\*{35}{l}}

{{Y}\_{k,j}} & = & {{\left( \frac{{{P}\_{k,j}}}{{{\beta }\_{k}}{{P}\_{j}}} \right)}^{1-\sigma }}{{Y}\_{j}} \\

\end{array}\]

Where ${{P}\_{k,j}}$ and ${{P}\_{j}}$ are price indexes, ${{\beta }\_{k}}>0$ is a sector-specific preference parameter, ${{Y}\_{j}}$ is total demand for imported goods, $\sigma >1$ is the elasticity of substitution between sectors.

Assume each country exports a specific national variety. Preferences within each sector $k$ between national varieties are assumed well represented by a CES utility function with the same $\sigma $ parameter as the intersectoral CES utility function. Intrasectoral demand for varieties exported by $i$ in $j$ in sector $k$ is:

\[\begin{array}{\*{35}{l}}

{{X}\_{k,ij}} & = & {{\left( \frac{{{p}\_{k,ij}}}{{{\gamma }\_{i}}{{P}\_{k,j}}} \right)}^{1-\sigma }}{{Y}\_{k,j}} \\

\end{array}\]

Where ${{\gamma }\_{i}}>0$ is a origin-country-specific preference parameter and ${{P}\_{k,j}}$ is the CES price index:

\[\begin{array}{\*{35}{l}}

{{P}\_{k,j}} & = & {{\left[ \sum\limits\_{i\ne j}{{{\left( \frac{{{p}\_{k,ij}}}{{{\gamma }\_{i}}} \right)}^{1-\sigma }}} \right]}^{1/(1-\sigma )}} \\

\end{array}\]

Defining $\frac{{{Y}\_{k,j}}}{{{Y}\_{j}}}={{\omega }\_{k,j}}$, we get:

\[\begin{array}{\*{35}{l}}

\frac{{{X}\_{k,ij}}}{{{Y}\_{j}}} & = & {{\omega }\_{k,j}}{{\left( \frac{{{p}\_{k,ij}}}{{{\gamma }\_{i}}{{P}\_{k,j}}} \right)}^{1-\sigma }} \\

\end{array}\]

Summing over all SITC 4-digit sectors:

\[\begin{array}{\*{35}{l}}

\sum\limits\_{k=1}^{K}{\frac{{{X}\_{k,ij}}}{{{Y}\_{j}}}}=\frac{{{X}\_{ij}}}{{{Y}\_{j}}} & = & \gamma \_{i}^{\sigma -1}\sum\limits\_{k=1}^{K}{{{\omega }\_{k,j}}}{{\left[ \frac{{{p}\_{k,ij}}}{{{P}\_{k,j}}} \right]}^{1-\sigma }} \\

\end{array}\]

The market share equation for aggregate bilateral trade as a function of the weighted average of sectoral relative prices of in is:



Changing notations:

\[\begin{array}{\*{35}{l}}

\frac{{{X}\_{ij}}}{{{Y}\_{j}}} & = & {{\kappa }\_{i}}\sum\limits\_{k=1}^{K}{{{\omega }\_{k,j}}}\frac{p\_{k,ij}^{1-\sigma }}{\sum\limits\_{l\ne j}{{{\kappa }\_{l}}}p\_{k,lj}^{1-\sigma }} \\

\end{array}\]

As this is a market share, it is reasonable to assume that the errors are multiplicative. We have to fit the following model on the data:

\[\begin{array}{\*{35}{l}}

\frac{{{X}\_{ij}}}{{{Y}\_{j}}} & = & {{\kappa }\_{i}}\sum\limits\_{k=1}^{K}{{{\omega }\_{k,j}}}\frac{p\_{k,ij}^{1-\sigma }}{\sum\limits\_{l\ne j}{{{\kappa }\_{l}}}p\_{k,lj}^{1-\sigma }} \\

\end{array}.{{e}^{{{\varepsilon }\_{i,j}}}}\]

Notice that we only have non-zero observations, as ${{p}\_{k,ij}}$ is only observed when there is a trade flow. We take logs to transform the errors into additive ones and estimate the following equation for each year with a non-linear least square procedure in STATA:

\[\begin{array}{\*{35}{l}}

\ln \left( \frac{{{X}\_{ij}}}{{{Y}\_{j}}} \right) & = & \ln \left( {{\kappa }\_{i}} \right)+\ln \left( \sum\limits\_{k=1}^{K}{\frac{{{Y}\_{k,j}}}{{{Y}\_{j}}}.}\frac{p\_{k,ij}^{1-\sigma }}{\sum\limits\_{l\ne j}{{{\kappa }\_{l}}}p\_{k,lj}^{1-\sigma }} \right) \\

\end{array}+{{\varepsilon }\_{i,j}}\]

This yields annual estimates of ${{\kappa }\_{i}}$ and $\sigma $[[28]](#footnote-28).

# Evolution of the Armington trade elasticity in 1963-2009

## The incidence of missing unit values

To estimate the market share equation on the COMTRADE dataset we need to tackle the question of missing information on trade flows and unit values (uv).

A first difficulty arises when the trade flow is observed but information on quantities is missing, and it is therefore not possible to compute the unit value. On average, lacking uv corresponds to 14% of total recorded trade in 1962-2009, with a gradual decrease from 17% to 10% between 1962-2000, and a subsequent increase back to 18% in 2001-2009. In 2001-2006 it is 13-15%, and about 18% in 2007-2009. We assume that information on quantities is missing due to imperfections in the data collection procedure, and that bilateral trade flows are observed with a similar degree of precision whether or not quantity had been recorded. To deal with missing uv, we impute prices from similar products using a stepwise price imputation procedure.

The stepwise price imputation procedure is as follows. The relative price of each source in the destination is constructed at the highest disaggregation level for each product and quantity unit in which the source is active, the *4’-digit* level. We then proceed level by level for aggregation: the relative price of the composite sectoral good of the source is constructed at the 4-digit level using the weighted average relative price observed at the 4’-digit level, with destination-specific weights for each variety of the 4’-digit good the source is active in. If no price is available at the 4-digit level, we move at the 3-digit level, etc. This improves the estimation of prices if one assumes that missing destination-specific relative prices at the 4’-digit can be approximated by the mean observed destination-specific relative price among the corresponding 4-digit group (and similarly at each aggregation level).

## Zero trade flows

A second difficulty arises when both quantity and trade data are missing. Zero trade flows (ztf) are a prevalent feature of the data while under model assumptions some trade should be observed in every sector *k* between all pairs *ij*.[[29]](#footnote-29) We assume that this information is missing because the underlying trade flow is positive but so small that it does not pass the threshold applied by the data collecting authorities (in UN COMTRADE this threshold corresponds to 1000 USD). Such flows, if recorded, would not substantially modify the distribution of observed market shares in the destination (the left hand side of equation ) because they are an order of magnitude smaller than observed trade.

We use the same stepwise price imputation for zero trade flows as in the case of missing unit values. This is problematic because statistically unobserved trade values must correspond to a higher cif price than the maximum observed price in the destination across all sources and sectors while by construction we postulate that unobserved relative prices in ztf sectors are equal to a weighted average relative price across sectors in which trade is observed. [[30]](#footnote-30)

This assumption would not bias our estimate if the underestimation factor were constant across exporters. This scalar would cancel out across sources, and the estimated substitutability parameter would correspond to the true parameter. Table 2 shows it is not the case. The share of ztf is strongly decreasing in market share, i.e. the underestimation factor is larger for small exporters (though they already have higher prices). As a result, for a given observed distribution of market shares, the underlying dispersion in relative prices of the composite good is greater than the observed dispersion in relative prices. This means that the estimated parameter $\tilde{\sigma }$ overestimates the true substitutability parameter $\sigma $.

Table 2 shows that the reduction in the share of ztf proceeds at quicker pace in 1962-2009 for small exporters: the coefficient for the interaction term for the market share and year is significant and positive. Table 3 presents the predicted share of ztf for four types of exporters in 1962 and 2009. For a very small exporter with .02% market share, the initial share of ztf is predicted to be .95, and it is reduced to .83 by 2009, i.e. a 12 percentage point decrease. Consider a relatively big exporter, with a 10% market share: its share of ztf is reduced from .72 to .65, a 7 percentage point decrease. As the gap between the share of ztf for big and small exporters is reduced overtime, the overestimation bias of $\tilde{\sigma }$ is progressively reduced.

Table 2: Proportion of zero trade flows as a function of market share

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| depvar: Share of ZTF | | | | | | |
|  | (1) | (2) |  | (3) | (4) | |
|  |  |  |  |  |  | |
| ms | -0.0401**\*\*\*** | -0.2446**\*\*\*** |  | -0.0427**\*\*\*** | -0.2573**\*\*\*** | |
|  | (0.0001) | (0.0134) |  | (0.0001) | (0.013) | |
| year | -0.0029**\*\*\*** | -0.0020**\*\*\*** |  | -0.0033**\*\*\*** | -0.0024**\*\*\*** | |
|  | (0.0000) | (0.0001) |  | (0.0000) | (0.000) | |
| *ms*\**year* |  | 0.0001**\*\*\*** |  |  | 0.0001**\*\*\*** | |
|  |  | (0.0000) |  |  | (0.000) | |
| constant | 5.3474**\*\*\*** | 3.5852**\*\*\*** |  | 6.0976**\*\*\*** | 4.2515**\*\*\*** | |
|  | (0.0335) | (0.1372) |  | (0.0366) | (0.134) | |
|  |  |  |  |  |
| Destination FE | NO | NO |  | YES | YES |
| Observations | 657001 | 657001 |  | 657001 | 657001 |

Notes: The share of ZTF is computed at the SITC 4-digit level. The estimation is conducted in PPML in order to include observations where ztf=0. The log of the market share is used in the estimation. Destination fixed effects are included in (3) and (4). Robust standard errors are in parentheses. \*\*\* p<0.01.

Table 3: Predicted share of ztf for exporters with different market share, 4-digit level

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| year | ms=0.02% | ms=1% | ms=10% | ms=28.7% |
| 1962 | 0.95 | 0.80 | 0.72 | 0.69 |
| 2009 | 0.83 | 0.71 | 0.65 | 0.62 |

Columns (1) and (4) correspond to the mean and to 2 st. deviations above the mean in the distribution of log market share. Columns (2) and (3) correspond to the mean and to 2 st. deviations above the mean in the distribution of market share.

Thus, the hypothesis we make on unobserved sectoral prices in ztf sectors does not always impede interpreting the evolution of the underlying substitutability parameter. In particular, because the overestimation bias is reduced overtime, if it is found that the estimated parameter increases in absolute value, this evolution necessarily provides a lower bound on the increase in the underlying substitutability parameter.

Figure 7 presents the results on the evolution of $\left( 1-\sigma \right)$ obtained when equation is estimated in annual cross-sections of the COMTRADE dataset. 2008 is obviously an outlier. However, even excluding 2008, the absolute value of trade elasticity has increased by 38% from 1962 to 2013. This corresponds to an annual increase of .6% per year.[[31]](#footnote-31) According the preceding discussion, this is a lower bound on the increase in the underlying substituability parameter.

Figure 7: Estimated (1−\[\tilde{\sigma }\] )



## Robustness checks

### Changing the dataset

We provide a robustness check by estimating the evolution of the heterogeneity parameter for aggregate bilateral trade on a different dataset. We use the BACI dataset which reports bilateral trade data at the HS-1992 6-digit disaggregation level for 1995-2009. The accuracy of the relative prices of country-composite goods constructed with this dataset is improved because the harmonization procedure applied by (Gaulier et Zignago 2010) in constructing BACI yields much better-quality unit values while substantially reducing the number of observations with lacking unit value. As a result, at the 6-digit level, less than 7% of total reported trade in BACI has missing unit values. This is reduced to 1-3% of total trade when the data is aggregated to the 4-digit level, as opposed to more than 10% in the raw COMTRADE data we originally used. Another advantage is that the share of ztf in BACI is stable in 1995-2009 as opposed to relatively strong fluctuations in the share of ztf overtime in our original dataset. The disadvantage of BACI is that it covers only a relatively short period compared to the years over which the distance puzzle exists. Obviously, we do not expect to reproduce exactly the results obtained with our original dataset because the trade classification and its level of aggregation are different.

Figure 8: Estimated (1−), BACI database

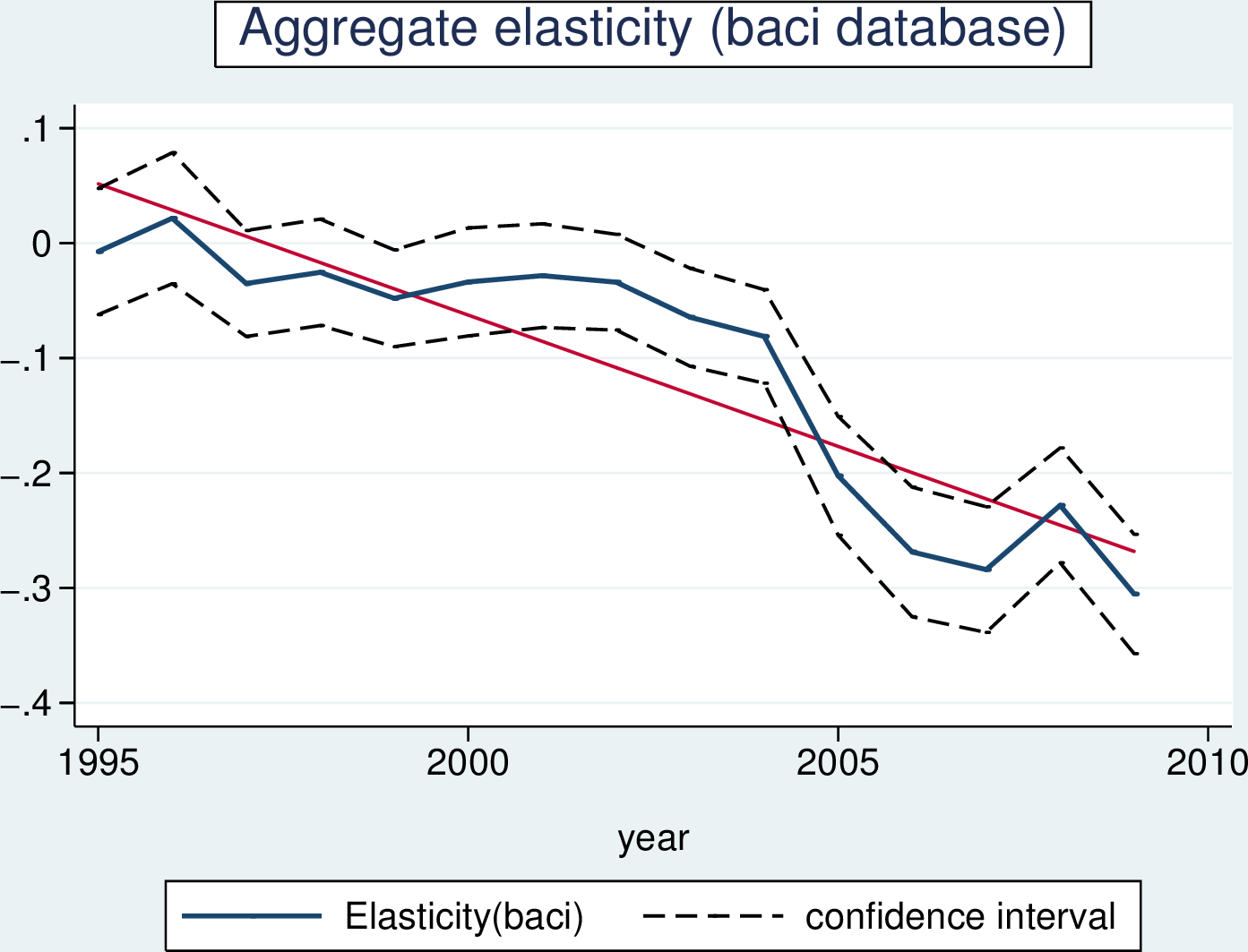


Figure 8 shows that our results hold: the elasticity parameter is found to increase in absolute value from 1995-2009. This can be compared with the equivalent period in our original dataset: the increase in the elasticity is much steeper on the BACI dataset. This finding supports the idea that our benchmark estimation likely provides a lower bound on the increase in the aggregate trade elasticity. However, the level of the elasticity estimated in 1995-1999 on BACI data is puzzling and suggests the existence of an attenuation bias. This is the focus of our second robustness check.

### Price instrumenting and the non-linear estimation of σ

#### Instrumenting procedure

In equation , it is possible that the estimate of $\sigma $ is downward-biased because of unobserved demand shifters that may be correlated with prices (Hummels et Schaur 2013). Specifically, whenever the supply curve has a finite slope, unobserved demand shocks will result in a simultaneous increase in the price and in the expenditure on sector *k* products. Further, even if the supply curve is perfectly elastic, measurement error may lead to a downward bias in the estimate of $\sigma $. This downward bias occurs whenever there is a systematic link between unobserved quality and observed unit values whereby higher observed unit values in sector *k* are associated with higher underlying quality and, consequently, higher expenditure on sector *k* products.[[32]](#footnote-32)

To check whether unobserved demand shifters correlated with prices are a source of concern in the estimation, we need an instrument that adequately captures exporter-specific shocks to sector *k* prices that are not demand-driven, such as exogenous shocks to the cost of inputs. We use adjusted past unit values as an instrument for current unit value. The adjustment is based on exporter-specific price shocks as measured by domestic price evolutions. Unfortunately, we do not have information on producer price indices at the SITC 4-digit level. Even at the aggregate level, PPI information is not available for most countries and years in our sample. We therefore settle for the price level of GDP and the price level of investment.

The price level of GDP will be a valid instrument if demand shocks in the importing country are the main source of price endogeneity, and the small country assumption holds. In this case, demand shocks in any market for products of a particular exporter will have no incidence on world prices of these products and, consequently, the price level of GDP in the exporting country will be independent of idiosyncratic demand shocks in the importing country. If however the small country assumption does not hold for certain importers, the price level of GDP could itself be a function of demand for exporter-specific products. Therefore, as a robustness check, we use the price level of investment as an alternative proxy for cost shocks to production because the price of investment is more likely to be determined by global demand for industrial goods and to be exogenous to unobserved demand shocks in any given market.

Information on the price level of GDP and the price level of investment is reported in the Penn World Table 9.0 for 182 countries in 1950-2015 in current US dollars (R. C. Feenstra, Inklaar, et Timmer 2015). For each variable, the price level is normalized to 1 in the USA in 2005. Information is provided for 113 countries in each year, and for the remaining countries between 10 and 51 years are covered. Thus, our sample of countries does not coincide perfectly with the countries in the Penn World Table. However, as it is the smallest exporters that drop out, the sample adjustment in terms of world trade coverage is minor.

The instrumenting procedure consists in exploiting past information on unit values and on changes in the cost of domestic inputs to replace observed unit values ${{p}\_{k,ij,t}}$ with predicted unit values ${{\hat{p}}\_{k,ij,t}}$.

We assume a stylized cost function in which the sector-specific cost is determined by an economy-wide cost measure ${{C}\_{it}}$ together with sector-producer specific characteristics summarized by the index ${{z}\_{k,i,t}}$ (> 0) and bilateral characteristics of trade costs ${{z}\_{ij,t}}$ (> 0). Denoting the time lag by $l$, we assume:

\[{{c}\_{k,ij,t}}={{C}\_{i,t}}.{{z}\_{k,i,t}}.{{z}\_{ij,t}}\]

We assume further that the cost component is well captured by the GDP or investment price level: ${{C}\_{i,t}}=P\_{i,t}^{v}$ where $v=\left\{ gdp,i \right\}$. Prices are a more or less sensitive to costs, depending on the competition conditions in each sector. The elasticity of prices to costs is \[{{\alpha }\_{k,t}}\] (>0). It is a measure of the path-through that depends on specific sector conditions. Prices are also dependent on consumer-sector-producer specific characteristics ${{z}\_{k,ij,t}}$ (> 0) that capture, for example, shocks to demand in $j$ for products from $i$ in sector $k$. As a result:

\[{{p}\_{k,ij,t}}={{\left( P\_{i,t}^{\nu }.{{z}\_{k,i,t}}.{{z}\_{ij,t}} \right)}^{{{\alpha }\_{k,t}}}}.{{z}\_{k,ij,t}}\]

Then, for each time-lag $l$, and assuming sector-specific price-setting conditions (i.e. \[{{\alpha }\_{k,t}}\]) constant between $t-l$ and $t$, we have:

\[\begin{align}

& {{p}\_{k,ij,t}}={{p}\_{k,ij,t-l}}{{\left( \frac{P\_{i,t-l}^{v}}{P\_{i,t-l}^{v}}.\frac{{{z}\_{k,i,t}}}{{{z}\_{k,i,t-l}}}.\frac{{{z}\_{ij,t}}}{{{z}\_{ij,t-l}}} \right)}^{{{\alpha }\_{k,t}}}}.\frac{{{z}\_{k,ij,t}}}{{{z}\_{k,ij,t}}} \\

& \Leftrightarrow \\

& \ln \left( {{p}\_{k,ij,t}} \right)=\ln \left( {{p}\_{k,ij,t-l}} \right)+{{\alpha }\_{k,t}}.\ln \left( \frac{P\_{i,t}^{v}}{P\_{i,t-l}^{v}} \right)+{{\alpha }\_{k,t}}.\ln \left( \frac{{{z}\_{k,i,t}}}{{{z}\_{k,i,t-l}}} \right)+{{\alpha }\_{k,t}}.\ln \left( \frac{{{z}\_{ij,t}}}{{{z}\_{ij,t-l}}} \right)+\ln \left( \frac{{{z}\_{k,ij,t}}}{{{z}\_{k,ij,t}}} \right) \\

\end{align}\]

Predicted unit values are obtained by regressing observed unit values on the product of lagged unit values and the change in the price level of domestic output (investment), assuming that the sum of the three other members of the sum follows a normal law. Our baseline equation for the first stage of the estimation for a given lag is:

\[\ln {{p}\_{k,ij,t}}-\ln {{p}\_{k,ij,t-l}}={{\alpha }\_{k,t}}\ln \left( \frac{P\_{i,t}^{v}}{P\_{i,t-l}^{v}} \right)+{{\varepsilon }\_{k,ij,t,l}}\]

We estimate this equation separately for each year of the sample. Hence, we allow the estimated coefficients to be year-specific. The identification assumption is that current shocks specific to the sector and to the pair (${{\varepsilon }\_{k,ij,t-l}}$) that may simultaneously drive up price and expenditure in year *t* are independent of lagged prices and changes in producer cost component.

The choice of the lag is associated with a trade-off. The shorter the lag, the more data we can use. However, if demand shocks in the destination are persistent, the covariance between the lagged price and the demand shock in the error term may remain positive if the first lag is used. Hence, we use a three-year lag in the baseline specifications.

For almost all years, and all specifications (there are a few exceptions at the beginning of the period) the path-through estimated in equation is statistically significant and positive. The R² is very small. That suggests that economy-wide domestic conditions explain a very small share of price and sector-specific price variations. Considering the dimension of the data, this is perhaps not surprising. Still, this may worry us as to the weakness of our instrument. Recall however that the instrument is actually the adjusted past unit value. Past unit values have a very strong correlation with present unit values. The correlation between adjusted past unit values and current unit values is slightly higher.

As a falsification test, we verify that variations of the unit price are not explained by past or future variations of domestic costs. We thus estimate the following equation:

\[\ln {{p}\_{k,ij,t}}-\ln {{p}\_{k,ij,t-l}}={{\alpha }\_{k,t}}\ln \left( \frac{P\_{i,t}^{v}}{P\_{i,t-l}^{v}} \right)+{{\beta }\_{k,t}}\ln \left( \frac{P\_{i,t+2}^{v}}{P\_{i,t+1}^{v}} \right)+\gamma \ln \left( \frac{P\_{i,t-3}^{v}}{P\_{i,t-4}^{v}} \right)+{{\varepsilon }\_{k,ij,t,l}}\]

### Instrumenting: motivation and results (old)

The results just presented are subject to caution if supply schedules are not horizontal.[[33]](#footnote-33) The demand elasticity parameter estimated in the market share equation would then be subject to attenuation bias due to not controlling for potentially positive and finite supply elasticities. This attenuation bias would not be problematic for analyzing the evolution of the substitutability parameter if only the level of the parameter were affected. The problem arises because, as shown by (R. Feenstra 1994), the attenuation bias also impacts the evolution of the parameter.

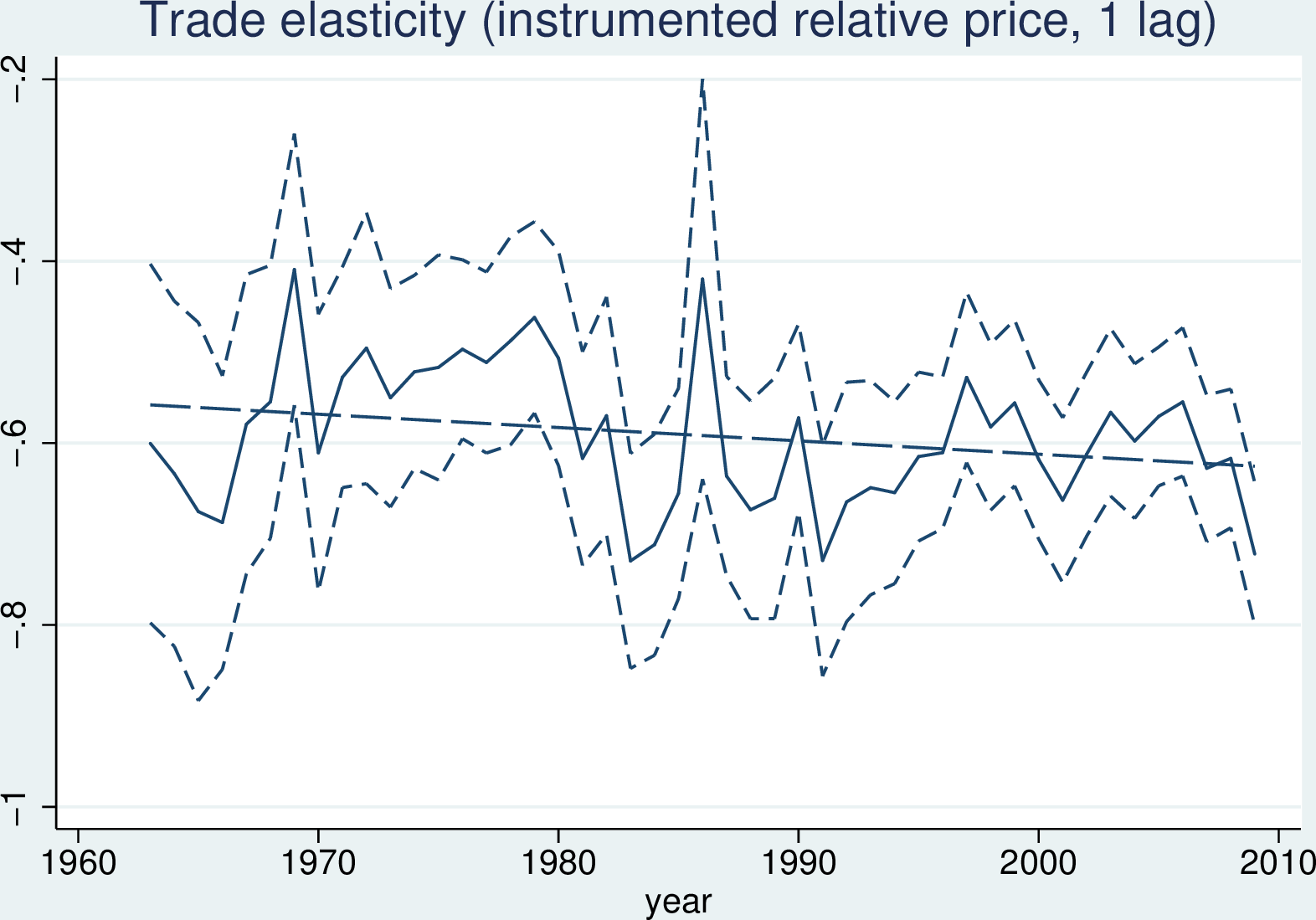
As explained in 2.3, our approach is different from the canonical one as we are keen on preserving the time dimension that is central to our analysis. We need an instrument that adequately captures exporter-specific shocks to the price of the composite good which are not demand-driven, such as exogenous shocks to inputs’ prices. We would like to use changes in the bilateral-specific real exchange rate. One possibility would be to use Producer Price Index (PPI) since it captures the evolution of prices faced by producers on the inputs’ side. Unfortunately, we do not have PPI data for most countries and years in our sample. We therefore settle for an alternative exporter-specific price level indicator: the GDP price level in current US dollars as reported in the Penn World Tables for 189 countries in 1950-2009.[[34]](#footnote-34)

The instrumenting procedure is the following. First, we compute relative prices for exporter-specific composite goods in each destination market using the stepwise price imputation procedure (see 3.1). Second, for each destination market, we compute the mean evolution of GDP price levels in current US dollars of its trading partners, weighted by their market shares in this destination. This amounts to computing the evolution of the relevant real exchange rate for each specific bilateral trade relation. Third, we compute a hypothetical relative price at time *t* for each exporter in each market as the product of its relative price at time (*t*−1) and the evolution of its GDP price level between *t* and (*t*-1) relatively to all other trading partners in this destination. Fourth, we predict the relative price of each exporter in each destination at time *t* by regressing its observed relative price on this hypothetical relative price. This gives an instrumented relative price for each exporter which depends only on its past relative price and the relative evolution of its GDP price level. Finally, we estimate equation using these instrumented relative prices instead of the observed relative prices.

It could be argued that allowing for just one lag inadequately captures the temporal relationship between shocks to inputs’ prices and their pass-through to the price of exported output. Indeed, if prices are relatively persistent, the instrumenting procedure would amount to little more than replacing observed prices in *t* with lagged observed prices in (*t*-1). We therefore also estimate equation using as instrument the evolution of each exporter’s GDP price level relatively to all other trading partners in the destination between (*t*-*s*) and *t* where *s*=1,...,10.

Results obtained with one lag (*s*=1) are shown in Figure 9. The absolute value of the substitutability parameter has increased by 13% in 1963-2009 while the level of the estimated parameter increases by 9% on average relatively to the estimate obtained with non-instrumented prices.

Figure 9 : Estimated (1−$\tilde{\sigma }$), instrumented relative price of composite good, 1 lag



This result is robust to increasing the number of periods in which the evolution of exports’ prices is predicted with the evolution of domestic prices. Thus, in 1972-2009, the elasticity increases by 20% when the instrument is constructed with one lag, and by 23% when the number of lags is 10 (see Appendix **Erreur ! Source du renvoi introuvable.**). The evolution of the parameter becomes steeper as we increase the number of lags. Therefore, it is likely that our estimate provides a lower bound on the increase in the true substitutability parameter.

## Is there a distance puzzle left?

This section has provided empirical evidence on the evolution of the aggregate substitutability parameter for world trade in 1963-2009. This substitutability parameter corresponds to the aggregate trade elasticity in the Armington framework. We find that this parameter has increased by 33% between 1963 and 2009 in the benchmark estimation, and by 13% when prices are instrumented. Both estimates are likely to be lower bounds on the increase in the true substitutability parameter. Section 1 has shown that the distance elasticity of trade has increased by 7% over the same period. Combining these two results, there is no distance puzzle in the framework of the Armington model in as much as the elasticity of trade costs to distance has decreased by at least 5-7% in 1963-2009.[[35]](#footnote-35) Increasing perceived substitutability of country-specific composite goods contributes to the increasing distance elasticity of trade.

The reduction in the elasticity of trade costs to distance is even more pronounced if we focus on 1970-2009. As shown by (Hummels 2007), this period is characterized by a new phenomenon: the fact that air transportation starts playing a substantial role in world trade. The instrumented Armington elasticity increases by 19% in this period while the evolution of the distance elasticity is best described as flat. It follows that the elasticity of trade costs to distance has decreased by at least 17% in 1970-2009.

What is the economic interpretation of an increasing substitutability parameter measured on aggregate data?

First, the degree of perceived similarity of country-composite goods may have increased. Since the 1960s, a growing number of countries started producing a set of goods similar to that of developed countries. This process has increased the number of available varieties and, potentially, their degree of similarity.[[36]](#footnote-36)

Second, composition effects may have lead to changes in the parameter estimated on aggregate data. If the reduction in trade barriers has led to the expansion in the range of traded goods, trade in previously non-traded sectors could modify measured substitutability of country-composite goods. Non-uniform reductions in sectoral trade costs would also modify the composition of world trade, leading to a change in the substitutability parameter measured on aggregate data. However, at first approximation, the rising importance of manufactures compared to primary products in world trade should have reduced substituability.

Ideally, we would like to separate out the impact of composition and sector-specific effects to quantify the net effect of increased perceived similarity of country-composite goods. This is however impossible because, as shown by (Imbs et Méjean 2013), the parameter estimated on aggregate data cannot be mimicked by a weighted average of sectoral parameters. The bottom line is that an increase in measured substitutability for country-composite goods is consistent with complex competition dynamics in price and quality documented by (Amiti et Khandelwal 2013) as well as with increased vertical specialization of countries within sectors documented by (Fontagné, Gaulier, et Zignago 2008).

# Conclusion

The estimated effect of distance in gravity equations has increased in the past fifty years despite substantial innovation in transportation and communication: this is the ‘distance puzzle’. Using COMTRADE 4-digit bilateral trade data in 1962-2009, this paper finds that the evolution of the elasticity of trade flows to trade costs, referred to as the ‘trade elasticity’, provides a direct explanation of the increasing distance elasticity of trade. Increased sensitivity of trade flows to relative prices has more than compensated the reduction in the elasticity of trade costs to distance.

The paper proceeds in three steps. First, it shows that the distance puzzle is a feature of our data by estimating yearly cross-section gravity equations. In the baseline estimation the distance coefficient has increased by 7% from 1962 to 2009. This result holds when we correct for changes in the sample of trading partners and the composition of world trade. Taking into account FTAs seems to solve the distance puzzle, but this might be an artefact of their growing importance: introducing FTAs dummies amounts to adding a time-growing number of proximity controls in the estimation.

Second, the paper suggests an *ad hoc* method of measuring structural heterogeneity in the Armington framework. In the main theoretical foundations of the gravity equation the distance coefficient is the product of the elasticity of trade costs to distance and a measure of heterogeneity. In the Armington framework, heterogeneity is inter-country and intra-sector. The trade elasticity corresponds to the degree of perceived substitutability of country-specific varieties of each good, which can be approximated by studying the relations between the price level and the market share of importers in destination markets.

Third, the paper estimates the evolution of the trade elasticity in the Armington framework, i.e. the substitution elasticity between country composite goods. It uses 4-digit unit values as proxies for sectoral prices. In our method, unobserved unit values for zero trade flows lead to an overestimation bias that is reduced over time. As the estimated elasticity still increases in absolute value this evolution provides a lower bound on the increase in the absolute value of the underlying trade elasticity. Once instrumented by bilateral real exchange rates, the estimated elasticity increases by 13% between 1963 and 2009. The evolution of the distance coefficient is thus compatible with a decrease of the elasticity of trade costs to distance of at least 5 to 7%. This reduction in the elasticity of trade costs to distance is even more pronounced if we focus on the period in which air transportation starts playing an important role in bilateral trade. We find that from 1970 to 2009 the elasticity of trade costs to distance has decreased by 17% while the perceived substitutability of countries’ product bundles has increased by at least 19%.

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2. KU Leuven [↑](#footnote-ref-2)
3. PSL, Université Paris-Dauphine, LEDa-DIAL UMR IRD 225, F-75016 Paris, France

   PSL, IRD, DIAL UMR IRD 225, F-75016 Paris, France

   SciencesPo, OFCE, F-75007 Paris, France [↑](#footnote-ref-3)
4. (Berthelon et Freund 2008; Combes, Mayer, et Thisse 2006; Brun et al. 2005; Buch, Kleinert, et Toubal 2004). [↑](#footnote-ref-4)
5. (Cairncross 1997; Levinson 2006; Friedman 2007). [↑](#footnote-ref-5)
6. (Santos Silva et Tenreyro 2011; Fally 2012) provide evidence on desirable properties of the PPML. Inadequacy of alternative non-linear estimators is discussed in (Bosquet et Boulhol 2009; Bosquet et Boulhol 2010). (Head et Mayer 2014) review properties of alternative estimators. [↑](#footnote-ref-6)
7. Using a non-linear estimator that controls for the mass of exporting firms (Larch, Norbäck, et Sirries 2013) find a decreasing distance elasticity in 1980-2006. They attribute the puzzle to the growing bias of the OLS estimate. [↑](#footnote-ref-7)
8. This leaves open the question of the estimator that correctly captures the level of the distance elasticity. (Head et Mayer 2013) argue that PPML gives too little weight to small trade flows characteristic of more distant partners. For (Santos Silva et Tenreyro 2006) small trade flows are more prone to measurement error. [↑](#footnote-ref-8)
9. (Head et Mayer 2013) propose a typology of persistent but unobserved trade costs. (Anderson et Wincoop 2004) provide a decomposition of total trade costs. (Daudin 2003; Daudin 2005) put forward that trade costs may have remained stable as a share of value added. [↑](#footnote-ref-9)
10. (Erkel-Rousse et Mirza 2002) do this exercise for just one point in time on a subsample of world trade flows. [↑](#footnote-ref-10)
11. (Berthelon et Freund 2008) work with 776 sectors defined at the SITC Rev.2 4-digit level. (Broda et Weinstein 2006) use time-series variation in prices and market shares for the set of exporters to the US market to get one value for the Armington elasticity in 1972-1988 and another value in 1990-2001. [↑](#footnote-ref-11)
12. The earliest available year is 1962. The estimation is conducted on import flows. We focus on 1963-2013 for consistency with the timeframe used in estimation of Armington trade elasticities in section 3. [↑](#footnote-ref-12)
13. See (Mayer et Zignago 2011) . The database is available at <www.cepii.fr>. We constructed bilateral distance and bilateral cost controls for East and West Germany, USSR, and Czechoslovakia. [↑](#footnote-ref-13)
14. COMTRADE itself covers between 70% to 90% of total world merchandise trade according to the WTO (<http://stat.wto.org/Home/WSDBHome.aspx>). As trade data is of better quality for imports, the estimation is conducted on import flows. [↑](#footnote-ref-14)
15. We split the sample in two subperiods, 1963-1990 and 1993-2009, to take into account country creation and disappearance in the early 1990s. [↑](#footnote-ref-15)
16. The superbalanced sample includes 37 countries listed in **Erreur ! Source du renvoi introuvable.**. The appendix discusses trade coverage. [↑](#footnote-ref-16)
17. This formulation is not specific to the Armington framework. See footnote 20 in (Eaton et Kortum 2002) and subsequent discussions of equivalence in (Arkolakis, Costinot, et Rodriguez-Clare 2012), (Head et Mayer 2013). [↑](#footnote-ref-17)
18. This assumption can be questioned, in particular with respect to excluded trade cost controls which vary as a result of trade policy decisions. We examine this question in **Erreur ! Source du renvoi introuvable.**. [↑](#footnote-ref-18)
19. We follow notation in HeadMayer2013. [↑](#footnote-ref-19)
20. The underlying annual growth rate is 0.10% in the full, and 0.44% in the superbalanced sample. [↑](#footnote-ref-20)
21. The opposite result holds in the loglinear specification (see HeadMayer2013). In OLS the decrease in the distance elasticity due to the elimination of small trade flows between distant partners trumps the increase in the distance elasticity of stable trade relationships. [↑](#footnote-ref-21)
22. The underlying annual growth rate is 0.29% in the full and 0.44% in the superbalanced sample. [↑](#footnote-ref-22)
23. Explained variation in the stable sample is 79% with the fixed, and 51% with the current product bundle. [↑](#footnote-ref-23)
24. App.**Erreur ! Source du renvoi introuvable.** provides details on each FTA and the years in which it appears in the sample. [↑](#footnote-ref-24)
25. The upper-tier elasticity measures substitutability of domestic products and an aggregate import good. The lower-tier one measures substitutability between importers of a given good. See (Sato 1967; Reinert et Shiells 1991; Saito 2004). [↑](#footnote-ref-25)
26. This assumes that the cif price is the consumer price in the importing country. This is not strictly true because custom duties are not included in the cif price. However, origin-specific variations in custom duties are much smaller than cif price variations. [↑](#footnote-ref-26)
27. When several quantity units are observed, the sector is defined at the product\*quantity-unit level. [↑](#footnote-ref-27)
28. Because of the way the procedure *nl* works in STATA, instead of minimizing , it minimizes  where  is the number of 4-digit sectors in which imports from  to  are recorded. As a result, we have to weight the regression by  to make its results comparable to those in part one. [↑](#footnote-ref-28)
29. The share of observed SITC 4-digit flows relatively to the total number of potential SITC 4-digit bilateral trade flows increases from 10% to 14% in 1962-2009. [↑](#footnote-ref-29)
30. An alternative method consists in imputing unobserved relative prices with some arbitrary price above the maximum observed in the destination. As ztf constitute 85-90% of all 4-digit trade flows, this method is problematic because results are driven by imputed rather than effectively observed prices. [↑](#footnote-ref-30)
31. The coefficient of the geometric fit is significant at 1% level, the 95% confidence interval is between 0.4% and 0.9% (not taking into account though the uncertainty around yearly estimates). [↑](#footnote-ref-31)
32. Another potential problem is linked to using per kg instead of per item prices. As discussed in (Hummels et Schaur 2013), unit values reflect product bulkiness, and bulkier products are more likely to be shipped via cheaper means of transportation. If products differ in bulkiness within the sector, unit value differences will overstate price differences and lead to a downward bias in the estimated elasticity. [↑](#footnote-ref-32)
33. (Broda et Weinstein 2006) find that supply elasticities are finite at the 4-digit level. On the other hand, (Magee et Magee 2008) find that the small country assumption may hold in the data in which case there would be no attenuation bias. [↑](#footnote-ref-33)
34. See (Heston, Summers, et Aten 2011). Our sample of countries does not coincide perfectly with the countries in the Penn World Tables. However, as it is the smallest exporters that drop out, the sample adjustment in terms of world trade coverage is minor. [↑](#footnote-ref-34)
35. The elasticity decreases by 5% when the evolution of $\rho $ is computed from the ratio of trends, and by 7% when it is computed as the trend of the ratios. [↑](#footnote-ref-35)
36. (Schott 2004) documents increased similarity in the set of exported goods of US trade partners while (Broda et Weinstein 2006) document the increase in the number of imported varieties since the 1970s. [↑](#footnote-ref-36)